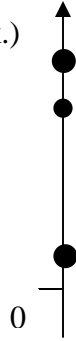


Sample test questions:

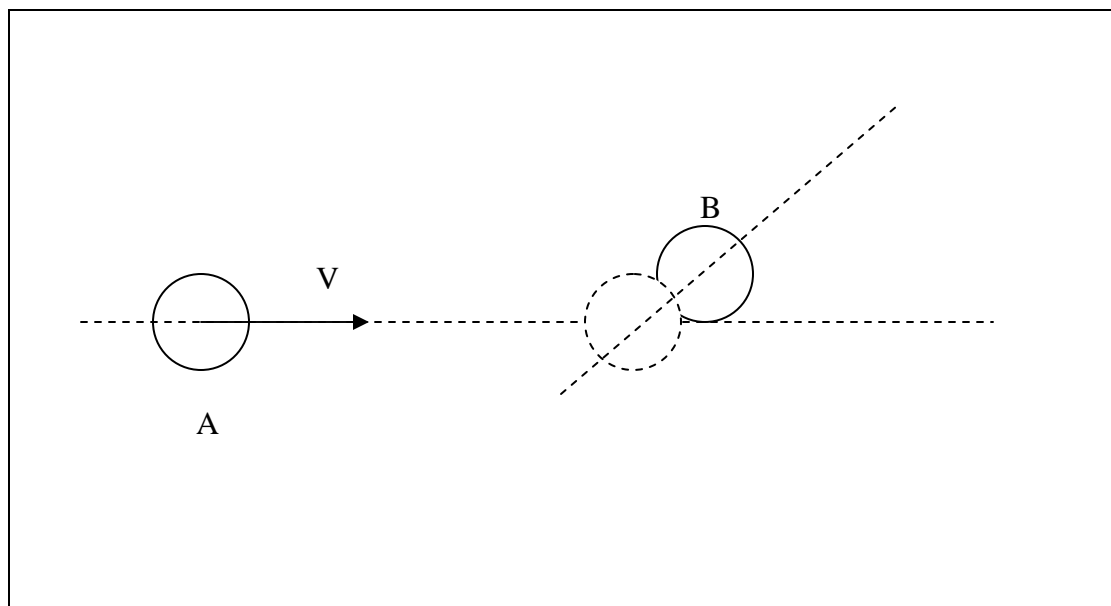
Multiple choices: (Only one answer is correct. Please choose the best answer you think.)

1. The drawing shows two 4.5 kg balls located on the y axis at 1.0 and 9.0 m, respectively; a third ball with a mass 2.3 kg is located at 6.0 m. what is the location of the center of mass of this system?
 - (a) 4.8 m
 - (b) 5.2 m
 - (c) 5.6 m
 - (d) 6.0 m
 - (e) 6.4 m
2. An object of mass $3m$, initially at rest, explodes breaking into two fragments of mass m and $2m$, respectively. Which of the following statements concerning the fragments after the explosion is true?
 - (a) They may fly off at right angles.
 - (b) They may fly off in the same direction.
 - (c) The smaller fragment will have twice the speed of the larger fragment.
 - (d) The larger fragment will have twice the speed of the smaller fragment.
 - (e) The smaller fragment will have four times the speed of the larger fragment.



Comprehensive questions:

A billiard ball, A, with an initial velocity of 3 m/s collides into a stationary billiard B at 30° angle elastically, as shown in the graph. What is the velocity of ball A after collision?



Answer:

1. B
2. C. (conservation of momentum)

Brief Solution:

1.

Since the two billiards had an elastic collision, both momentum and energy were conserved in the process.

For momentum conservation:

$$m_1 (3\text{m/s}) = m_1 v_{1x} + m_2 v_{2x}$$

And

$$0 = m_1 v_{1y} + m_2 v_{2y}$$

using $v_{2x} = v_2 \cos 30^\circ$, $v_{2y} = v_2 \sin 30^\circ$, $m_1 = m_2$, one can easily get:

$$3 = v_{1x} + v_2 (\cos 30^\circ)$$

And

$$v_{1y} = -v_2 \sin(30^\circ)$$

Using energy conservation, one has:

$$\frac{1}{2} m_1 (3\text{m/s})^2 = \frac{1}{2} m_1 v_{1x}^2 + \frac{1}{2} m_1 v_{1y}^2 + \frac{1}{2} m_2 v_2^2$$

Plug the previous two expressions into the last equation, one can solve out v_2 as 2.31 m/s

Therefore, $v_{1x}=1$ m/s and $v_{1y}=1.15$ m/s.

This is correspondent to a $v_1=1.53$ m/s at $\tan^{-1}(1.15/1)=49^\circ$ downward.