

# Graphs (Matroids) with $(k \pm \epsilon)$ -edge-disjoint spanning trees (disjoint bases)

Ping Li \*, Hong-Jian Lai\*, Yanting Liang\*

February 28, 2011

## Abstract

In this research project we consider these problems:

- (i) For a graph  $G$  that does not have  $k$ -edge-disjoint spanning trees, we are to determine the minimum number of edges that must be added to result in a graph with  $k$ -edge-disjoint spanning trees. Likewise, given a matroid  $M$  that does not have  $k$ -disjoint bases, we want to find a matroid  $M'$  that contains  $M$  as a restriction such that  $M'$  has  $k$  disjoint bases and such that  $|E(M') - E(M)|$  is minimized.
- (ii) For a graph  $G$  with  $k$  disjoint spanning trees, we are to determine which edge  $e$  such that  $G - e$  also has  $k$  edge-disjoint spanning trees. Likewise, for a matroid  $M$  with  $k$  disjoint bases, characterize the elements  $e$  such that  $M - e$  also has  $k$  disjoint bases.

Researches on these problems will be reported.

---

\*Department of Mathematics, West Virginia University, Morgantown, WV 26506