The Helly and Radon Numbers in Multipartite Tournaments

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Abstract

One of the goals in convexity theory is to study the relationship between various convex invariants. For two-path convexity in a multipartite tournament T, we study the relationship between the Helly number h(T), the Radon number r(T), and the rank d(T). In the case that T is clone-free, we found that h(T) = r(T) = d(T) whenever $d(T) \ge 4$ and that h(T) = r(T) except perhaps when h(T) = 2and r(T) = 3. The results are not as pretty in general multipartite tournaments, but we still get some nice results.