Strongly Chordal k-trees

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A graph is a k-tree if if is chordal, every maximal clique has order k + 1and every minimal separating set has order k. In this talk, we consider the subset of k-trees that are also strongly chordal. We give some preliminary results on the structure of such graphs and prove that every strongly chordal k-tree with toughness $\tau > \frac{k+1}{4}$ is hamiltonian for $k \ge 2$. This result is best possible for k = 3 and seemingly better than best possible for k = 2, but has considerable room for improvement when k is large.