## Wile E. Coyote's Roller Skate Chase



Click on the image to view an clip of this episode.
With the help of some Acme rocket powered roller skates, Wile E. Cote will attempt to snatch the Road Runner. We will use the TI-84 Plus CE and parametric mode to simulate this real-world scenario.

1. Press mode and select Parametric and Simultaneous Graphing. Please make sure you are also in Radians.
2. Press zoom 4: ZStandard for the standard window.

Press window.
Notice the standard settings are

3. Press $\mathrm{y}=$.

Enter $x(t)=t, y(t)=3$ which will animate the Road Runner's path.
Press 1 until you can't any more, then press enter. Optional: Press $\square$ (84CE) or enter (84) to change the graph style to animated path ( ${ }^{(1)}$ ).

$0 \leq t \leq 2 \pi$ in steps of Tstep $=\frac{\pi}{24}$ with $-10 \leq x \leq 10$ by $-10 \leq y \leq 10$.


Press graph. Press trace and to observe the graph.

5. Optional (TI-84CE only):

Press 2nd [format] to access the Graph Format menu. Place your cursor on the Background Spinner Press $\square$ on the spinner to select Image 1 .

Then press $\Delta$ or $\nabla$.
Image 1 should be highlighted.


Press graph to see Road Runner cross the bridge.

8. Work with a partner with the same calculator model and graph style settings as yours.

Clear or deselect Wile E. Coyote's previous formulas graph in $x 2 y 2$. Describe how does he move for each. Sketch a graph of $x(t)$ for each below. What symmetry do you notice in the graphs and the speeds?
Partner A enters: $x(t)=e^{t}-10$
Partner B enters: $x(t)=e^{-t}-10$

$$
y(t)=3
$$

Description of how he moves (left, right, speeds up slows down):
Description of how he moves (left, right, speeds up slows down):


9. On your grapher pick two of the parametric equations below. Assign one to Road Runner and another for Wile and enter them both into your grapher, using the same window as before (and the same graph styles for each). Observe how each moves across the bridge. Notice when each speeds up and slows down and which one overtakes the other. Which formulas go back and forth? Make connections with the graph of $x(t)$ vs $t$.
Optional: Construct your own set with $-10 \leq x(t) \leq 10$ for $-10 \leq t \leq 10$.

$$
\begin{array}{lll}
x(t)=10-2|t| & x(t)=10-0.2 t^{2} & x(t)=0.01 t^{3} \\
y(t)=3 & y(t)=3 & y(t)=3 \\
& & \\
x(t)=10 \cos (0.1 \pi t) & x(t)=10 \sin (0.1 \pi t) & x(t)=\tan \left(\frac{\pi t}{20}\right) \\
y(t)=3 & y(t)=3 & y(t)=3
\end{array}
$$



Imagine the graph of the function $x(t)$ vs $t$ is crushed by an Acme Anvil and is flattened onto the horizontal line $y=3$.

# Wile E. Coyote's Flying Wing Suit 

With the help of a handy Acme flying wing suit and some bird seed, Wile E. Cote will attempt to drop down from the sky to snatch the distracted Road Runner.


1. We will use the parametric equations $x(t)=t^{51}, y(t)=3$ for the Road Runner's path. Before entering these into your grapher, discuss the following with your group.
a. Describe the behavior of the graph of $x(t)=t^{51}$, shown to the right, for $-1<t<1$. What do you notice about his speed?
b. Describe the behavior of the graph of $x(t)$, shown to the right, for $t<-1$ and $t<-1$. What do you notice about his speed?
c. Report the $x$ and $y$ value of his path $t=0 . x=$ $\qquad$ $y=$ $\qquad$ What is Road Runner doing?

2. We will use the parametric equations $x(t)=e^{-t}, y(t)=e^{-t}+3$ for Wile E. Coyote's path. Before entering these into your grapher, discuss the following with your group.
a. i. Eliminate the parameter to report the path in terms of $y$ and $x$.

$$
y(x)=\ldots \quad \text { (This is called an explicit form.) }
$$

ii. What kind of function is this?
iii. Complete: As $x$ increases, the graph of $y(x)$ $\qquad$
As $t$ increases, the graph of $y(x)$ $\qquad$ .
b. Report the domain and range of Wile E. Coyote's motion path ( $y$ vs $x$ ) you found in Question 2ai, restricted to $-2 \leq t \leq 2$.

|  | Domain | Range |
| :--- | :--- | :--- |
| Exact |  |  |
| Approximate (to 1 decimal place) |  |  |


| $x=e^{-t}$ | $y=e^{-t}+3$ |
| :---: | :---: |
| 10 | ${ }^{10}$ - |
| 8 - | - |
|  | ${ }^{8}$ |
| 6 | 6 - |
| 4 |  |
| - | 2 |
|  |  |
| $-2-2$ | -2 |
| -2- | -2- |
| -4- | -4- |
| ${ }_{-6}{ }^{-}$ | -6- |
|  |  |
| -8- | -8- |
| ${ }_{-10}{ }^{-}$ | $-10^{-}$ |
|  |  |
| WINDOW |  |
| Tmin $=-2$$T_{\text {max }}$d |  |
| Tstep $=0.01$Xmin $=-10$ |  |
|  |  |
|  |  |
| $Y_{\text {min }}=-10$ |  |
| $Y_{\text {max }}=10$ |  |
| $Y_{\text {scl }}=1$ |  |

