

Suppose we have a limit such as $\lim_{x \rightarrow 0} (86 \tan^{-1} 209x) \left(\frac{1}{11x} \right)$ which is of the form $0 \cdot \infty$

To rewrite it in the form $\frac{0}{0}$ we use the fact that $A \cdot \frac{B}{C} = \frac{A}{\frac{1}{B}} \cdot \frac{B}{C} = \frac{AB}{C}$.

$$\lim_{x \rightarrow 0} (86 \tan^{-1} 209x) \left(\frac{1}{11x} \right) = \lim_{x \rightarrow 0} \left(\frac{86 \tan^{-1} 209x}{11x} \right) \text{ is now in the form } \frac{0}{0}.$$

Use L'Hopital's Rule:

$$\begin{aligned} \lim_{x \rightarrow 0} \left(\frac{86 \tan^{-1} 209x}{11x} \right) & \underset{\substack{\uparrow \\ \text{LH}}}{=} \lim_{x \rightarrow 0} \frac{\frac{d}{dx} 86 \tan^{-1} 209x}{\frac{d}{dx} 11x} = \lim_{x \rightarrow 0} \frac{86 \frac{1}{1 + (209x)^2} \cdot \frac{d}{dx} 209x}{11} \\ & = \lim_{x \rightarrow 0} \frac{86 \frac{1}{1 + (209x)^2} \cdot 209}{11} \\ & = \lim_{x \rightarrow 0} \frac{1}{11} \cdot 86 \cdot \frac{1}{1 + (209x)^2} \cdot 209 \\ & = \frac{86 \cdot 209}{11} \lim_{x \rightarrow 0} \frac{1}{1 + (209x)^2} \\ & = \frac{86 \cdot 209}{11} \cdot \frac{1}{1 + (0)^2} = \boxed{1634} \end{aligned}$$