

Suppose we have a limit such as  $\lim_{x \rightarrow \infty} \frac{e^{ugly} - 1}{ugly}$  where  $\lim_{x \rightarrow \infty} ugly = 0$  and  $ugly$  is a function of  $x$ .

Then the limit is of the form  $\frac{0}{0}$ .

Use L'Hopital's Rule:

$$\lim_{x \rightarrow \infty} \frac{e^{ugly} - 1}{ugly} \stackrel{\text{LH}}{=} \lim_{x \rightarrow \infty} \frac{\frac{d}{dx} e^{ugly} - \frac{d}{dx} 1}{\frac{d}{dx} ugly} = \lim_{x \rightarrow \infty} \frac{e^{ugly} \cdot \frac{d}{dx} ugly - 0}{\frac{d}{dx} ugly} = \lim_{x \rightarrow \infty} e^{ugly} = e^0 = 1$$