## The Velocity of Thomas the Tank Engine

Thomas the Tank Engine is $d=f(t)$ miles from his boss Sir Topham Hatt, where $t$ is given in hours. The graph of $d=f(t)$ is shown for $0 \leq t \leq 7$. The derivative, $d^{\prime}(t)$ is Thomas' instantaneous velocity $v(t)$ at time $t$.
Recall $d^{\prime}(t)$ also gives Thomas' trajectory of movement.

1. Near what integer values of $t$ is Thomas' velocity $v(t)=d^{\prime}(t)=0$ ? Hint: look at when the tangent line is horizontal. $t=$ $\qquad$
2. a. On what intervals of $t$ is $v(t)=d^{\prime}(t)>0$ ? $\qquad$
b. At these times, is Thomas traveling toward Sir Topham Hatt or away?
$d(t)$
miles from Sir Topham Hatt

3. a. On what intervals of $t$ is $v(t)=d^{\prime}(t)<0$ ? $\qquad$
b. At these times, is Thomas traveling toward Sir Topham Hatt or away?
4. Discuss any values of $t$ for which there are any absolute extremum (max or min) of $v(t)=d^{\prime}(t)$ on $0 \leq t \leq 7$.
5. Which of the following (dashed) graphs below is the velocity $v(t)=d^{\prime}(t)$ of Thomas? Select one. Explain your reasoning.
A.

B.

C.

D.

E. 1

F.

6. Interpret what the dashed graph in Choice F represents in the context of Thomas' trip.
