

I'm Heidi!

Important Ideas:

Memory Tip for the Quotient Rule: "Heidi comes second."

$$\frac{d}{dx} \left(\frac{\text{Hi}}{\text{Lo}} \right) = \frac{\text{Lo dee Hi} - \text{Hi dee Lo}}{\text{LoLo}}$$

From <http://www.foxsports.com/buzzer/story/craziest-moments-in-nfl-history-the-heidi-game-081314>

$$\left(\frac{u}{v} \right)' = \frac{u'v - v'u}{v^2}$$

↑
Division

Assume $v^2 \neq 0$
which means $v \neq 0$

The derivative of a quotient is a quotient
" " " " " has a numerator similar to the product rule with a minus sign instead of a plus sign.

Simplify first if possible.

Check Your Understanding

1. $p(t) = \frac{10t^2}{t^2 + 50} \Rightarrow p'(t) = \frac{1000t}{(t^2 + 50)^2}$ see class notes

2. $y(x) = \frac{3x^2 + 2\sqrt{x}}{x^2} = \frac{3x^2}{x^2} + \frac{2x^{1/2}}{x^2} = 3 + \frac{2x^{1/2}}{x^{4/2}} = 3 + 2x^{1/2 - 4/2} = 3 + 2x^{-3/2}$

$$y'(x) = \frac{d}{dx} 3 + \frac{d}{dx} (2x^{-3/2})$$

$$= 0 + 2 \cdot (-3/2) x^{-3/2 - 1/2}$$

$$= -3x^{-5/2} \text{ or } \frac{-3}{x^{5/2}}$$

You CAN use the Quotient Rule, but in this case, simplifying first is the best choice!

TIP: Write this down each time you use it

3. $y(x) = \frac{3x^2}{4 \ln x} = \frac{\text{hi}}{\text{lo}}$

$$y'(x) = \frac{\text{lo dee hi} - \text{hi dee lo}}{\text{lolo}} = \frac{4 \ln x \frac{d}{dx} 3x^2 - 3x^2 \frac{d}{dx} 4 \ln x}{(4 \ln x)^2} = \frac{(4 \ln x)(6x) - 3x^2(\frac{4}{x})}{(4 \ln x)^2}$$

$$= \frac{24x \ln x - 12x}{(4 \ln x)^2} = \frac{12x(2 \ln x - 1)}{(4 \ln x)^2} = \frac{3 \cdot 4x(2 \ln x - 1)}{4 \cdot 4 (\ln x)^2} = \frac{3x(2 \ln x - 1)}{4 \ln^2 x}$$

4. The table below gives values of f, g, f' , and g' at selected x -values.

x	$f(x)$	$f'(x)$	$g(x)$	$g'(x)$
-1	6	5	3	-2
1	3	-3	-1	2
3	1	-2	2	3

Let $h(x) = \frac{f(x)}{g(x)}$. Find $h'(-1)$.

$$h'(x) = \frac{\text{lo dee hi} - \text{hi dee lo}}{\text{lolo}} = \frac{g(x)f'(x) - f(x)g'(x)}{(g(x))^2}$$

$$h(-1) = \frac{(3)(5) - (6)(-2)}{3^2} = 3$$

$g(-1) = 3$
 $f'(-1) = 5$
 $f(-1) = 6$
 $g'(-1) = -2$