The graph of $f$ and $f^{\prime}$ are shown below. Complete the blanks, using the graph of $f^{\prime}$ to help you.
A horizontal tangent line to $f$ at a point $P$ occurs where the two sided limit of the derivative $f^{\prime}$ ' is $\qquad$ .

Vertical tangent lines of $f$ are where the one sided limits of the derivative $f^{\prime}$ at $P$ are infinities of
$\{\overline{\text { opposite signs, the same sign }}\}$
$f$ has cusps where the one sided limits of the derivative $f^{\prime}$ at $P$ on each side are
\{opposite, the same\} ${ }^{\text {. }}$
$f$ has vertical cusps are where the one sided limits of the derivative $f^{\prime}$ at $P$ on each side are infinities of $\qquad$ .
What do you notice?



