

This illustration shows how worksheet Illustration1.xlsx is adapted to accommodate a large funding situation with J=12 Category 2 features and $2^{12} = 4,096$ possible funding scenarios.

Figure 2.1

Partial image of the evaluation sheet of illustration2.xlsx.

	F	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	BY	BZ	CA
10				Decatenated 0/1 characters of v and the 0/1 values of f2,j, j=1,...,12														
11	Scenario reference, v	Binary form of v														Funded Category 2 features, j	r	Funding cost ¹
2556	2544	00001001	11110000	0	0	0	0	1	1	1	1	1	0	0	1	5 6 7 8 9 12	6	14.209
2557	2545	00001001	11110001	1	0	0	0	1	1	1	1	1	0	0	1	1 5 6 7 8 9 12	7	14.489
2558	2546	00001001	11110010	0	1	0	0	1	1	1	1	1	0	0	1	2 5 6 7 8 9 12	7	14.561
2559	2547	00001001	11110011	1	1	0	0	1	1	1	1	1	0	0	1	1 2 5 6 7 8 9 12	8	14.841
2560	2548	00001001	11110100	0	0	1	0	1	1	1	1	1	0	0	1	3 5 6 7 8 9 12	7	14.584
2561	2549	00001001	11110101	1	0	1	0	1	1	1	1	1	0	0	1	1 3 5 6 7 8 9 12	8	14.864
2562	2550	00001001	11110110	0	1	1	0	1	1	1	1	1	0	0	1	2 3 5 6 7 8 9 12	8	14.936
2563	2551	00001001	11110111	1	1	1	0	1	1	1	1	1	0	0	1	1 2 3 5 6 7 8 9 12	9	15.216

¹ \$M.

For the funding situation of Table 1 of the manuscript with I=11 and j=1,...,12, the Evaluation tab of Illustration1.xlsx was adapted in the following ways. The Fill feature of Excel[®] was used to enter respectively the values of v (=0,1,...,4095) in cells F12, F13, ...,F4107. The cell formulae of K43-AP43 were then copied to cells K44-AP4107 producing the Evaluation sheet of Illustration2.xlsx. The copying converted the v of cells F12-F4107 to binary forms appearing in G12-J4107 with cell entries I12-J4107 relevant to the J=12 of this illustration, see above Figure 2.1. The outcomes of the conversions are the 0/1 values indicating exclusion/inclusion of Category 2 feature j(=1,...,12) in funding scenarios v=0,1,...,31 according to the labels j=1-12 appearing in cells K11-V11. Aspects of each scenario v are calculated in cells BY12-CA4107 including the funding cost of scenario v in column CA. Figure 2.1 above is a partial image of the Evaluation sheet of Illustration2.xlsx where rows 2556-2563 display the outcomes of stepwise additions of features j=1, 2, 3 to the indices 5 6 7 8 9 12 of scenario v=2544 in row 2556. The cell contents of BX12-CA4107 of the Evaluation sheet appear in the Results sheet in cells A12-D4107. The same contents appeared in cells F12-I4107 of the same sheet, were changed to values, then sorted by r in ascending order and scenario cost in ascending order within sorted r. The least costly funding scenarios for r=0,1,...12 Category 2 features are summarized in Table 2.1 below.

Table 2.1

The least cost scenarios of illustration 2.

r	0	1	2	3	4	5	6	7
Least Cost (\$M) of r Funded Category 2 Features	11.069	11.349 j=1	11.701 j=1,2	12.076 j=1-3	12.474 j=1-4	12.881 j=1-5	13.356 j=1-16	13.844 j=1-7
r	8	9	10	11	12			
Least Cost (\$M) of r Funded Category 2 Features	14.364 j=1-8	14.900 j=1-9	15.519 j=1-10	16.201 j=1-11	16.915 j=1-12			

If \$12M are available for funding Category 1 and Category 2 features, as many as r=2 Category 2 features may be funded; for \$13M, at most r=5; for \$14M, r=7; for \$15M, r=9; and for \$16M, r=10. The

funding of all $r=12$ Category 2 features requires \$16.915M. For the situation with a funding cap of \$13M, the five Category 2 features $j=1-5$ constitute the least costly scenario at \$12.881M. Suppose during review a new consideration in addition to the funding cap of \$13M is identified. There are eight scenarios with $r=5$ and funding costs between \$12.881M and \$13M, see cells G806-I813 in the Results sheet of Illustration2.xlsx. Among them, features $j=1-5$ appear in various combinations, albeit in only eight ways. If the new funding consideration is satisfied by at least one of the eight, a feasible scenario is identified. Otherwise, either fewer than five features can be funded or the new consideration cannot be accommodated within the \$13M funding cap. The outcomes presented in the Results sheet are helpful in examining funding considerations of this kind.

For a large spreadsheet such as Illustration2.xlsx, a Calculator is given to facilitate investigation of the consequence (e.g., cost and other considerations) of funding particular /discrete Category 2 features of interest. See cells J1-K7 of the Evaluation sheet of Illustration2.xlsx for the Calculator. Given the Category 2 features composing a scenario of interest, the Calculator identifies v and makes it unnecessary to search a long spreadsheet for the details thereof. To use the Calculator, enter indices j for the funded features of interest in cell K4 with separating commas, e.g., 2,5,12. The corresponding values of v and the scenario cost are returned respectively in cells K5 and K6. With v , additional details of the scenario can be found in the row of the Evaluation sheet in which v appears. For example, suppose the scenario with funded features $j=9,12$ are of interest to the analyst. With the entry 9,12 in cell K4, $v=2304$ and the cost \$12.319M are returned in cells K5 and K6 respectively. Because the Category 2 feature costs for this illustration are in ascending order with respect to $j=1,2,\dots,12$, the least costly single funding feature to add to the $j=9,12$ of scenario $v=2304$ is feature $j=1$. The entry 1,9,12 in cell K4 returns $v=2305$ and the funding cost \$12.599M in cells K5 and K6 respectively. The least costly pair addition to scenario with $j=9,12$ is $j=1,2$. Entry of 1,2,9,12 in cell K4 returns $v=2307$ and the funding cost \$12.951M. If the funding cap is less than \$12.951M, there is no feasible funding addition to the scenario with $j=1,9,12$. If other funding criteria applied and cell formulae were created for their evaluation by the user and included among the cell formulae for each v , their status would appear in the row corresponding to the returned v of cell K4. Illustration 3 that follows addresses such a situation. Note that alternative funding scenarios with $j=9,12$ appear in the vicinity of $v=2304$.