

Summation Notation of Riemann Sums

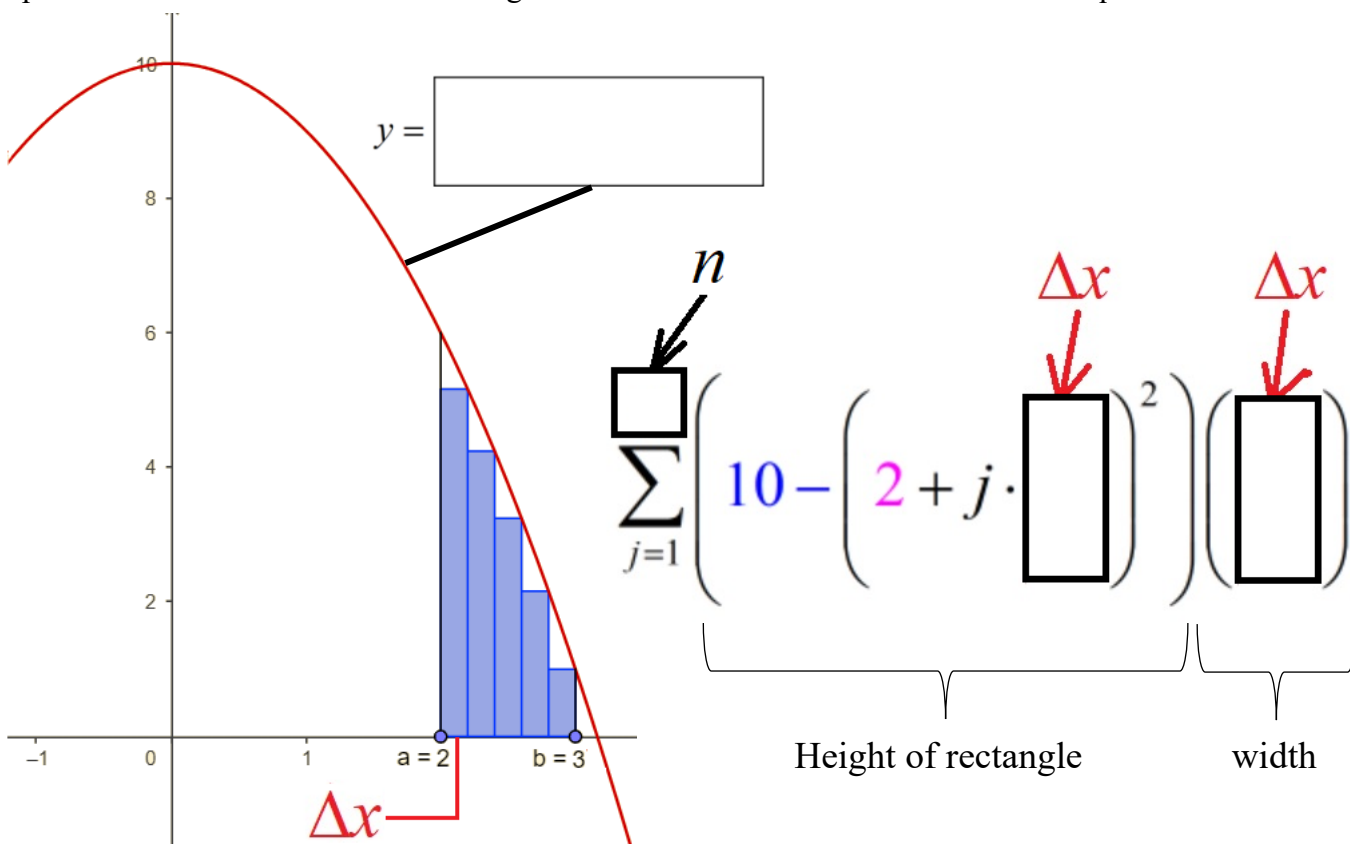
$$1. \lim_{n \rightarrow \infty} \sum_{j=1}^n \left(4 \left(1 + j \cdot \frac{10}{n} \right)^3 + 2 \right) \left(\frac{10}{n} \right) = \int_1^{11} (4x^3 + 2) dx$$

$$2. \lim_{n \rightarrow \infty} \sum_{j=1}^n \left(\left(2 + j \cdot \frac{5}{n} \right)^3 + 1 \right) \left(\frac{5}{n} \right) = \int_2^7 (x^3 + 1) dx$$

$$3. \lim_{n \rightarrow \infty} \sum_{j=1}^n \left(4 \left(5 + j \cdot \frac{2}{n} \right) - 2 \right) \left(\frac{2}{n} \right) = \int_5^7 (4x - 2) dx$$

$$4. \lim_{n \rightarrow \infty} \sum_{j=1}^n \left(3 \left(2 + j \cdot \frac{3}{n} \right) + 1 \right) \left(\frac{3}{n} \right) = \int_2^5 (3x + 1) dx$$

Complete the boxes. The area below is a right Riemann sum with $n = 5$ subintervals of equal width Δx .



If the number of subintervals n were to grow without bound, i.e., $n \rightarrow \infty$, then the sum would approach the actual area represented by

$$A = \int_{\boxed{}}^{\boxed{}} \left(\boxed{} \right) dx$$