

- 2. Interpret your answer to the previous question in practical terms. Select one.
 - A. The cost to go from producing 10 items to 11 items is greater than the cost to go from producing 60 to 61 items.
 - B. The cost to go from producing 60 items to 61 items is greater than the cost to go from producing 10 to 11 items.
 - C. The cost of producing 60 items is greater than the cost of producing 10 items.
- 3. The graph of R(x) and C(x) is shown. The cost function is $C(x) = 0.02x^3 - 2.4x^2 + 100x$

If items sell for \$36, write the revenue function

$$R(x) =$$

- 4. Use the graph to complete the blanks. Once production begins, the company will first break even when they make _____ items and then again when they make _____ items.
- 3300 3000 2700 2400 2100 1800 1500 1200 900 600 300 20 30 40 50 60 70 80 90 10 100 Number of items, x

C

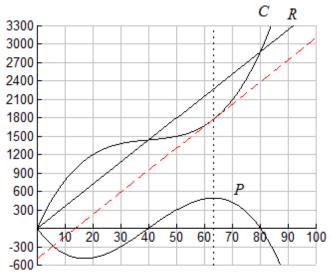
R

- 5. For what production values will the company produce a profit?
- 6. The company will choose to produce more items when marginal revenue exceeds marginal costs. Why?

Report: R'(x) =

- 7. Consider production levels at x = 50 and x = 70. Use the graph to answer the following:
 - **a.** Does the marginal revenue exceed marginal cost if they produce x = 50 items? A. Yes B. No
 - **b.** Does the marginal revenue exceed marginal cost if they produce x = 70 items? A. Yes B. No

- 8. The curve $C(x) = 0.02x^3 2.4x^2 + 100x$, the line R(x) = 36x, the profit function P(x), and the tangent line to C(x) at the value of $x \approx 63$ are sketched below.
 - **a.** No calculations are necessary to answer these. At a production level of $x \approx 63$ where *P* is maximum, what is the exact slope of the tangent line to P(x)? P'(63) = ______ what is the exact slope of the tangent line to R(x)? R'(63) = ______ what is the exact slope of the tangent line to C(x)? C'(63) = ______
 - **b.** Explain the relationship between the marginal profit P'(63), the marginal revenue R'(63), and the marginal cost C'(63)at the production level $x \approx 63$ when the profit is maximum. Sketch tangent lines to each at $x \approx 63$.



Number of items, x

A man named Archimedes looked at shaded areas like these and wondered, "Are these shaded areas the same?" What do you think?

Although it is not necessary to answer the questions in this activity, we have by subtraction:

$$P(x) = R(x) - C(x) = 36x - (0.02x^3 - 2.4x^2 + 100x)$$
$$= -0.02x^3 + 2.4x^2 - 64x$$
$$= -0.02x(x - 40)(x - 80)$$

