## Bug on a Circular Track

Suppose a bug travels along the path of a circle.
We know that the distance from A to B is $x$ units.


If the bug walks counterclockwise from $A$ to $C$, express the distance the bug walks in terms of $x$. What angle was spanned during the bug's trip?
1.

$m \overparen{A B C}=\frac{3 x}{2}$
What angle was spanned? $270^{\circ}$
$\left(\frac{3 x}{2}=x+\frac{1}{2} x\right.$ since $\frac{1}{2} x$ corresponds to $\left.90^{\circ}\right)$

$m \overparen{A B C}=\underline{\frac{11 x}{6}}$
What angle was spanned? $330^{\circ}$
$\left(\frac{11 x}{6}=2 x-\frac{1}{6} x=\frac{12}{6} x-\frac{1}{6} x\right)$
$330^{\circ}=360^{\circ}-30^{\circ}$

$m \overparen{A B C}=\underline{\frac{4 x}{3}}$
What angle was spanned? $240^{\circ}$
$\left(\frac{4 x}{3}=x+\frac{1}{3} x\right.$ since $\frac{1}{3} x$ corresponds to $\left.60^{\circ}\right)$
$240^{\circ}=180^{\circ}+60^{\circ}$
5.

$m \overparen{A B C}=\underline{\frac{5 x}{4}}$
What angle was spanned? $225^{\circ}$
$\left(\frac{5 x}{4}=x+\frac{1}{4} x\right.$ since $\frac{1}{4} x$ corresponds to $\left.45^{\circ}\right)$

$$
225^{\circ}=180^{\circ}+45^{\circ}
$$


$m \overparen{A C}=\frac{\frac{5 x}{6}}{}$
What angle was spanned? $150^{\circ}$ $\left(\frac{5 x}{6}=x-\frac{1}{6} x\right.$ since $\frac{1}{6} x$ corresponds to $\left.30^{\circ}\right)$ $150^{\circ}=180^{\circ}-30^{\circ}$

Need more practice? Try the following.
6.

$m \overparen{A C}=\frac{\frac{x}{2}}{}$

$m \overparen{A B C}=\underline{\frac{7 x}{6}}$
8.


$$
m \overparen{A C}=\frac{\frac{x}{3}}{}
$$

What angle was spanned? $90^{\circ}$


What angle was spanned? $210^{\circ}$
What angle was spanned? $\quad 60^{\circ}$


$$
m \overparen{A C}=\frac{\frac{x}{6}}{}
$$

What angle was spanned? $30^{\circ}$

$$
m \overparen{A B C}=\frac{7 x}{4}
$$

What angle was spanned? $315^{\circ}$
11.


$$
m \overparen{A C}=\frac{\frac{x}{4}}{}
$$

What angle was spanned? $45^{\circ}$


$$
m \overparen{A C}=\frac{3 x}{4}
$$

What angle was spanned? $135^{\circ}$

